Abstract

Motivated by various new applications of computational symmetry in computer vision and in an effort to advance machine perception of symmetry in the wild, we organize the third international symmetry detection challenge at ICCV 2017, after the CVPR 2011/2013 symmetry detection competitions. Our goal is to gauge the progress in computational symmetry with continuous benchmarking of both new algorithms and datasets, as well as more polished validation methodology. Different from previous years, this time we expand our training/testing data sets to include 3D data, and establish the most comprehensive and largest annotated datasets for symmetry detection to date; we also expand the types of symmetries to include densely-distributed and medial-axis-like symmetries; furthermore, we establish a challenge-and-paper dual track mechanism where both algorithms and articles on symmetry-related research are solicited. In this report, we provide a detailed summary of our evaluation methodology for each type of symmetry detection algorithm validated. We demonstrate and analyze quantified detection results in terms of precision-recall curves and F-measures for all algorithms evaluated. We also offer a short survey of the paper-track submissions accepted for our 2017 symmetry challenge.

1. Introduction

The real world is full of approximate symmetries appearing in varied modalities, forms and scales. From insects to mammals, intelligent beings have illustrated effective recognition skills and smart behaviors in response to symmetries in the wild [9, 15, 38, 48], while computer vision algorithms under the general realm of computational symmetry [24] are still lagging behind [13, 25].

Our Symmetry Detection in the Wild challenge, affiliated with the International Conference in Computer Vision (ICCV) 2017 in Venice, Italy, is the third in a series of symmetry detection competitions aimed at sustained progress quantification in this important subfield of computer vision. The first symmetry detection competition [51], funded through a US NSF workshop grant, was held in conjunction with CVPR 2011, and offered the first publicly available benchmark for symmetry detection algorithms from images. The second symmetry competition, held during CVPR 2013 [22, 52], started to build comprehensive databases of real world images depicting reflection, rotation and translation symmetries respectively. In addition, a set of standardized evaluation metrics and automatic evaluation algorithms were established, solidifying the computational foundation for validating symmetry detection algorithms.

A historic overview of symmetry detection methods can be found in [25, 32]. There has been much recent work in symmetry detection since the last symmetry competition in 2013 [22], including new deterministic methods [2, 46, 49], deep-learning methods [14, 42], and other learning-based methods [45]. New applications include Symmetry reCAPTCHA [13], 3D reconstruction [8, 12, 43], image segmentation [4, 19], and rectification and photo editing [27, 37]. Many of these algorithms are featured in our challenges as baseline algorithms. Levinshtein et al. [18] detected straight, ribbon-like local symmetries from real images in a multiscale framework, while Lee et al. [17] extended the framework to detect curved and tapered local symmetries. Pritts et al. [37] detect reflection, rotation and translation symmetry using SIFT and MSER features. The symmetries are found through non-linear optimization and RANSAC. Wang et al. [49] use local affine in-
variant edge correspondences to make their algorithm more resilient to perspective distortion contours. Teo et al. [45] detect curved-reflection symmetry using structured random forests and segment the region around the curved reflection. Sawada and Pizlo [39] exploit mirror symmetry in a 2-D camera image for 3-D shape recovery.

Motivated by various new applications of computational symmetry in computer vision, our third challenge expands our training/testing data sets to include 3D data, establishing the most comprehensive and largest annotated datasets for symmetry detection to date. We expand the types of symmetries to cover reflection, rotation, translation [25] and medial-axis-like symmetries in 2D and 3D synthetic and real image data, respectively. We also distinguish symmetry annotations between discrete, binary pixel labels and densely-distributed, continuous firing fields reflecting a gradient in degrees of symmetry perception. We have further refined our evaluation method to include F-measures in all standardized precision-recall curves for comparison.

In terms of the symmetry challenge organization, we have established a challenge-and-paper dual track mechanism where both algorithms and articles on symmetry-related research are solicited. For the challenge track, we have quantitatively evaluated 11 challenge-track submissions against 13 baseline algorithms. In paper track, we have accepted five paper-track submissions after an extensive review process. Detailed information, datasets and results of this symmetry challenge can be found on the workshop website.

2. Symmetry Challenge Track

We have divided our evaluation of the datasets in the symmetry challenge track into sparse versus dense/continuous labels, as well as 2D versus 3D symmetries.

2.1. General Evaluation Methods

For all challenge track evaluations, we use the standard precision-recall and F-score evaluation metrics [14, 22, 29, 47]. Precision measures the number of true positives: this is the number of detected medial points that are actually labeled as positives in the ground-truth:

\[ P = \frac{\text{true positives}}{\text{true positives} + \text{false positives}}. \]  

(1)

Recall measures the number of ground-truth positives that are successfully recovered by the algorithm:

\[ R = \frac{\text{true positives}}{\text{true positives} + \text{false negatives}}. \]  

(2)

Intuitively, precision is a measure of the accuracy of each detection, while recall measures detection completeness. These two measures give us a quantitative means of evaluating each algorithm. To gain further insight into the differences between the algorithms, we can evaluate precision and recall by altering threshold values in the evaluation or prediction confidences to create a plot of a PR-curve that illustrates the trade-off between precision and recall.

One can summarize the performance of an algorithm (and select the optimal threshold) using the harmonic mean of precision and recall, which is called the F-measure or F-score:

\[ F = \frac{2 \cdot P \cdot R}{P + R}. \]  

(3)

F-measure offers a convenient and justified single-value score for system performance comparison.

2.2. 2D Symmetry - Sparse Evaluation

The 2D sparse evaluated symmetry competition includes challenges on the detection of reflection and translation symmetry. The total number of images and symmetries for each task is shown in Table 1.

<table>
<thead>
<tr>
<th>2D Challenge Sparse</th>
<th>Type</th>
<th># Images</th>
<th># Symmetries</th>
</tr>
</thead>
<tbody>
<tr>
<td>Reflection</td>
<td>single</td>
<td>100/100</td>
<td>100/100</td>
</tr>
<tr>
<td></td>
<td>multiple</td>
<td>100/100</td>
<td>384/371</td>
</tr>
<tr>
<td>Translation</td>
<td>frieze</td>
<td>50/49</td>
<td>79/85</td>
</tr>
</tbody>
</table>

Table 1. The total number of images and symmetries within each 2D challenge in the training/testing sets.

2.2.1 Reflection and Translation Datasets

We have expanded and added new data sets beyond previous symmetry competitions [22]. The images are collected from the Internet and are annotated by symmetry researchers. For reflection symmetry, we divide the analysis into images containing either a single symmetry or multiple reflection symmetries. For translation, we tested the state-of-the-art algorithm(s) for 1D translation (frieze) symmetry.

The reflection symmetry annotations are line segments defined by two endpoints (Figure 1). Each translation symmetry annotation is a grid of points connected to create a lattice of quadrilaterals (Figure 2). For baselines, reflection uses Loy and Eklundh [26] and Atadjanov and Lee [3], and translation uses Wu et al. [54]. The evaluation metrics for each of these are similar to the previous symmetry competition [22].

Reflection Evaluation Metrics For the evaluation of reflection axis detection, we measure the angle difference between the detected and ground-truth axes and the distance from the center to the ground truth line segment. We use the same threshold values t1 (angle difference) and t2 (distance) used in [22]. Multiple detections for one ground truth
Figure 1. Example annotations of the 2D Reflection dataset. Blue lines are reflection symmetry axes.

Figure 2. Example annotations of the 1D translation (frieze) symmetry dataset.

axis are counted as one true positive detection, but none of them is counted as a false positive. We vary the confidence of the detections in order to create a precision-recall curve for each algorithm.

**Translation Evaluation Metric** We use the same distance-minimizing cost-function to align the detected and ground truth lattices as [35]. A detected quadrilateral tile is correct if it is matched with a ground truth lattice tile and the ratio of the matched tile areas is between 40% and 200%. We calculate the tile-success-ratio ($TSR$) [22] for each detected lattice. Similar to [22], we calculate true positives as images where a lattice is detected with a $TSR > \tau$, where $\tau$ is a threshold we vary from $[0,1]$. False positives are images where the best detected lattice has $TSR \leq \tau$, and false negatives are images where there was no lattice detected in the image.

2.2.2 Sparse Evaluation Results

The results for the reflection symmetry challenge are shown in Figures 3 and 4. Baseline methods achieve the best results on both single (Atadjanov and Lee [3] $F=0.52$) and multiple (Loy and Eklundh [26] $F=0.30$) reflection symmetry detections with respective highest $F$-measures. Loy and Eklundh [26] has shown robust performance on various datasets, including our previous competition. Atadjanov and Lee is one of the state-of-the-art methods reported in the literature. Elawady [11] shows a higher recall rate than others on the single symmetry dataset and is the top-performing method among all challenge submissions on both 2D reflection symmetry detection datasets.

For 1D translation symmetry, the baseline outperformed the submission of Michaelsen and Arens [30], Elawady et al. [11], Loy and Eklundh [26] (baseline), and Atadjanov and Lee [3] (baseline).

2.3. 2D Symmetry - Dense Evaluation

For dense evaluation the annotation is a binary map and the algorithm output is a confidence map, thresholded at multiple values to create the PR curve, with both of the maps have the same size as the input image (Figure 6. The evaluation is conducted per pixel rather than per reflection
Figure 5. PR curve on 1D Translation (Frieze) Symmetry Dataset. The algorithms tested are the challenger, Michaelsen and Arens [30], and the baseline Wu et al. [54].

Figure 6. Examples of the original image, dense annotations map (both overlaid and by itself), and an algorithm’s confidence map overlaid on the image. The ground truth is evaluated by comparing each pixel from the annotation and each pixel from the algorithm output. The top row image is from the Sym-COCO dataset and the algorithm is from Funk and Liu [14]. The bottom row image is from the BMAX500 dataset and the algorithm is from Tsogkas and Kokkinos [47].

2.3.1 Sym-COCO

The Sym-COCO task challenges algorithms to detect human perceived symmetries in images from the MS-COCO dataset [20] and the ground truths are collected via Amazon Mechanical Turk. The details on the collection and the creation of the ground truth labels are described in Funk & Liu [13, 14]. The dataset contains 250 training and 240/211 testing images for reflection/rotation (the same testing set as [14]) indicated in Table 2. The current state-of-the-art baseline algorithm is the deep convolutional neural network from Funk & Liu [14] (Sym-VGG and Sym-Res). We also compare against Loy and Ek-lundh’s algorithm [26] (LE), Tsogkas and Kokkinos’s algorithm [47] (MIL), the Structured Random Forest method of Teo et al. [45] (SRF), the Deep Skeleton method of Shen et al. [41, 42] (LMSDS,FSDS), and the challenge submission from Michaelsen and Arens [30].

This challenge and dataset are unique because they are based on human perception rather than the 2D symmetry contained within the image data. This goes beyond the mathematical definition of symmetry because the human perception of symmetry is invariant to out-of-plane rotation and incomplete symmetries. Some example images with labels are shown in Figure 7.

Figure 7. Example annotations of reflection (lines) and rotation (circles) from the Sym-COCO dataset.

2.3.2 Medial Axis Detection

For the task of medial axis detection we use two datasets recently introduced in the community. Since manually annotating medial axis/skeleton annotations in natural images with high precision can be cumbersome and time-consuming, we followed a practical approach that has been adopted in previous works [40, 41, 42, 47]. Specifically, we apply a standard binary skeletonization technique [44] on the available segmentation masks to extract ground-truth medial axes that will be used for training and evaluation. In this way, we obtain high-quality annotations for both location and scale of each medial point.

Below we list dataset statistics in more detail and highlight their differences.

SK-LARGE was introduced in [41], which consists of 1491 cropped images from MS-COCO [20] (746 train, 245 validation, 500 testing). The objects in SK-LARGE belong to a variety of categories, including humans, animals (e.g., birds, dogs and giraffes), and man-made objects (e.g., planes and hydrants).

BMAX500 is the second dataset used for the Medial Axis Detection challenge. It was introduced in [46] and is built on the popular BSDS500 dataset [1, 28]. BMAX500 contains 500 images that are split into 200 images for training, 100 images for validation, and 200 images for testing.

The original set of BSDS500 annotations contains segmentations collected by 5-7 human annotators per image, without any object class labels. As a result, there is no way
to distinguish between foreground and background, which makes BMAX500 an appropriate benchmark for evaluating a more general, class-agnostic medial axis detection framework. This is an important difference with respect to the SK-LARGE dataset, which is particularly focused on object skeletons.

### 2.3.3 Dense Evaluation Metrics

The algorithms examined in this part of the challenge output a real-valued map of probabilities or “symmetry/medial point strength” at each location in the image, rather than binary yes/no decisions. We turn this soft confidence map into a binary result of detected reflection symmetry/medial axis, by thresholding it at different values and plot the precision-recall curves as described in Section 2.1.

**Detection slack.** Both the ground-truth and the detected medial axes are thinned to single-pixel width in order to standardize the evaluation procedure. Now, consider two false positives returned by the tested algorithm, which are 1 pixel and 10 pixels away from a ground-truth positive. It would be unreasonable to penalize both of these false detections in the same way, since the first one is much closer to a true reflection symmetry axis/medial point.

---

**Table 2. The total number of images in the dense evaluation dataset, if the datasets have foreground (fg) or background (bg) distinction in the segmentations, and the number of symmetries.**

<table>
<thead>
<tr>
<th>Dataset</th>
<th># Images train/valid/test</th>
<th>fg/bg distinction</th>
<th># Symmetries train/test</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sym-COCO [14]</td>
<td>250/–/240</td>
<td>–</td>
<td>1535/1469</td>
</tr>
<tr>
<td>BMAX500 [46]</td>
<td>200/100/200</td>
<td>no</td>
<td>–</td>
</tr>
<tr>
<td>SKLARGE [41]</td>
<td>746/245/500</td>
<td>yes</td>
<td>–</td>
</tr>
</tbody>
</table>

---

**Figure 10. PR curve for the Sym-COCO Reflection dataset** for the 240 images and all GT labels (solid line) and for the subset of 111 reflection symmetry images with GT labels containing at least 20 labelers (dashed line), and the maximum F-measure values (dot on the line). The algorithms are the challenger Michaelsen and Arens [30] (MA), Funk and Liu [14] (Sym-VGG and Sym-Res - the baselines), Loy and Eklundh [26] (LE), Tsogkas and Kokkinos [47] (MIL), Teo et al. [45] (SRF), and Shen et al. [42] (FSDS).

We “forgive” such wrong yet reasonable detections by introducing a detection slack: all detected points within $d$ pixels from a ground-truth positive are considered as true positives. We typically set $d$ as 1% of the image diagonal [29].

### 2.3.4 Dense Evaluation Results

The Sym-COCO reflection challenge results are shown in Figure 10. The scores are the mean precision and recall, calculated among the images. The new challenger algorithm by Michaelsen and Arens [30] did not fare well in the competition and was surpassed by other algorithms. The algorithms which incorporate learning using additional images from outside this training set faired much better (all but Loy and Eklundh [26] and Michaelsen and Arens [30]) and the deep learning approaches (Funk & Liu [14] and Shen et al. [42]) predictably did the best. Funk & Liu [14], the baseline algorithm, took the top spot in the competition.

The results for medial axis detection are shown in Figures 11 and 12. The challenger algorithms beat the baseline algorithms for both datasets. In general, we observe that recent methods based on supervised deep learning outperform other learning-based and unsupervised, bottom-up approaches [47, 46].

---

### 2.4. 3D Symmetry

This part of the symmetry detection challenge only considers reflection symmetries of single 3D objects or within larger 3D scenes given as polygonal meshes.
2.4.1 Datasets and Annotation

The 3D dataset is split according to the following three different properties:

- **Synthetic vs. Real Data:** The annotation of real data is costly while large labeled synthetic datasets, which are often required for learning-based methods, can be easily obtained. Therefore, it is natural to select a combination of the two. The synthetic data is a collection of free, publicly available 3D models obtained from Archive3D [50]. The real datasets are kinect scans of real world scenes and are taken from the publicly available datasets that accompany two papers by Choi et al. [5, 6] as well as from the work of Speciale et al. [43].

- **Global vs. Local Symmetries:** The difference between global and local symmetries is that the symmetry property respectively holds either for the entire domain or only for a local region of the domain. In the literature, local symmetries are sometimes also called partial symmetries [31, 32].

- **Training vs. Test Data:** The test and training datasets have similar properties and data statistics. Corresponding ground truth data is made publicly available for the training dataset. Furthermore, performance evaluations on the test dataset will be performed upon request and subsequently published on the workshop website [53].

Figure 13 depicts some example scenes from the 3D dataset. The total number of scenes and symmetries for each task is shown in Table 3.

3D Synthetic Data Annotation. The synthetic data for global symmetries only contains single objects. Ground truth symmetries were found by sampling a set of symmetry planes and rejecting the ones for which the planar reflective symmetry score [36] is below a threshold. These objects are originally axis-aligned which may bias learning-based methods. We therefore provide a dataset of over 1300 axis-aligned objects and their annotations as well as their randomly rotated counterparts. The synthetic data for local symmetries is a collection of scenes composed of objects from the global symmetry dataset. The scenes were gen-
<table>
<thead>
<tr>
<th>3D Challenge</th>
<th>Type</th>
<th># Scenes</th>
<th># Symmetries</th>
</tr>
</thead>
<tbody>
<tr>
<td>Global Reflection</td>
<td>Synthetic</td>
<td>1354/441</td>
<td>1611/614</td>
</tr>
<tr>
<td></td>
<td>Real</td>
<td>20/20</td>
<td>21/22</td>
</tr>
<tr>
<td>Local Reflection</td>
<td>Synthetic</td>
<td>200/200</td>
<td>1939/2239</td>
</tr>
<tr>
<td></td>
<td>Real</td>
<td>21/21</td>
<td>44/46</td>
</tr>
</tbody>
</table>

Table 3. The total number of scenes and symmetries within each 3D challenge in the training/testing sets.

3D Real Data Annotation. The real world data was annotated manually with the help of a 3D editor and model viewer that directly overlays the semi-transparent geometry of the reflected scene. In this way, one can instantly assess the quality of the fit while adjusting the symmetry plane.

2.4.2 Evaluation Metrics

Similar to the 2D case, the 3D planar reflective symmetries are evaluated according to the position and orientation of the symmetry plane with respect to the ground truth. A correct detection (true positive) is credited if both the position of the symmetry plane center and the orientation are sufficiently close to the ground truth plane.

Let \((c, n)\) denote a symmetry plane given by the center point \(c \in \mathbb{R}^3\) on the plane and the plane’s normal vector \(n \in \mathbb{R}^3\), and let \((c_{GT}, n_{GT})\) be the corresponding ground truth symmetry. The symmetry is rejected if the angular difference between the symmetry normals is above a threshold \(\theta\), i.e. if \(\arccos(|n \cdot n_{GT}|) > \theta\). In practice, symmetries are given by three points \(x_0, x_1, x_2 \in \mathbb{R}^3\) which span the symmetry plane and also define a parallelogram that bounds the symmetry. Center point and normal are then given by \(c = \frac{1}{2}(x_1 + x_2), n = (x_1 - x_0) \times (x_2 - x_0)\). A symmetry is also rejected if the distance of the tested center \(c\) to the ground truth plane restricted to the bounding parallelogram is larger than a threshold: \(\|c - \Pi_{GT}(c)\|_2 > \tau\).

Precision-recall curves are generated by linearly varying both thresholds within the intervals \(\theta \in [0, 45^\circ]\) and \(\tau \in [0, 2]\). 

\[\min\{x_1 - x_0, x_1 - x_0, x_{1GT} - x_{0GT}, x_{1GT} - x_{0GT}\}\]

2.4.3 Results

Ecins et al. [10] submitted results for the real and synthetic test data set for local symmetries, which are shown in Figure 14 and Figure 15, respectively. The curve in Figure 14 is very short since there are not many variations due to the small size of the test dataset. Generally, the method computes symmetries with high accuracy for the ones it has detected. Figure 16 presents the results by Cicconet et al. [7] on the synthetic global test dataset.

3. Symmetry Paper Track

In the paper track of the workshop, full-length submissions were each reviewed by two members of the Organizing and/or Advisory Committees. In all, five papers were accepted for inclusion in the proceedings and presentation at the workshop.

In “Wavelet-based Reflection Symmetry Detection via Textural and Color Histograms” [11], Elawady et al. address the problem of detecting global symmetries in an image, in which extracted edge-based features are used to vote for symmetry axes based on color and texture information in the vicinity of the extracted edges.

In “SymmSLIC: Symmetry Aware Superpixel Segmentation” [34], Nagar and Raman offer a new twist on the su-
perpixel segmentation problem. If a set of corresponding pixels can be detected that exhibit approximate reflective symmetry about an axis, these points can serve as seeds for a SLIC-inspired superpixel segmentation algorithm where superpixels that encompass these symmetric seeds are simultaneously grown such that they, too, are symmetric.

In “SymmMap: Estimation of 2-D Reflection Symmetry Map with an Application” [33], Nagar and Raman compute a symmetry map representation consisting of two components: the first specifies, for each pixel, the location of its symmetric counterpart, while the second provides a confidence score for the mapping.

In “On Mirror Symmetry via Registration and the Optimal Symmetric Pairwise Assignment of Curves” [7], Cicconet et al. address the problem of detecting the plane of reflection symmetry in $R^n$ by registering the points reflected about an arbitrary symmetry plane, and then inferring the optimal symmetry plane from the parameters of the transformation mapping the original to the reflected point sets.

In “Hierarchical Grouping Using Gestalt Assessments” [30], Michaelsen and Arens describe a framework for using various types of symmetry (e.g., reflection, Frieze repetition, and rotational symmetry) to organize nonaccidental arrangements (Gestalten) into hierarchies that take into account image location, scale, and orientation.

4. Conclusions

Our evaluation of 11 different symmetry challenge track submissions against 13 baseline algorithms gives us a glimpse of the state-of-the-art of symmetry detection algorithms in computer vision. It is somewhat surprising that among the six algorithms evaluated, Loy and Eklundh’s algorithm of ECCV 2006 [26] remains competitive in detecting reflection symmetries on 2D images, in particular on detecting multiple reflection symmetries (F=0.30), while for detecting a single reflection symmetry in an image the baseline algorithm of Atadjanov and Lee [17] is the best (F=0.52). On frieze pattern detection from images, the F-scores of both baseline [54] and challenger [30] are relatively low (F=0.19-0.20). Seven algorithms are evaluated on the Sym-COCO dataset for reflection symmetry detection, for which the Funk and Liu [14] CNN baseline algorithm trained with human labels stands out (F=0.38-0.41). Moving on to medial-axis detection on real images, the good news is that the challengers RSRN [21] (F=0.64) and SegSkel [23] (F=0.73) beat the baseline algorithms as the winner on the BMAX500 and SKLARGE datasets respectively, yet they still score worse than humans (F=0.80). The 3D symmetry detection algorithms [7, 10] evaluated in this symmetry challenge demonstrated high promise on synthetic and real data sets respectively. But larger dataset and more algorithms are needed for a more comprehensive validation and comparison in the future.

There seems to be a general trend of an ascending order in symmetry detection performance of learning-based algorithms, deep-learning methods, and human, which suggests that we have much to learn from human perception. Though progress has been made, detecting symmetry in the wild has proven to be a real challenge facing the computer vision community and, more generally, the artificial intelligence community. We anticipate that future advancements on mid-level machine perception will benefit from the outcome (algorithms, labeled datasets) of our ICCV 2017 Detecting Symmetry in the Wild Challenge.

5. Acknowledgements

The authors would like to thank the rest of our 2017 ICCV Symmetry Challenge organizing team, all members of our advisory committee, all reviewers, and all contenders. A special thanks to Microsoft for sponsoring our 2017 Symmetry Challenge Cash awards. This work is supported in part by an US NSF CREATIV grant (IIS-1248076), NSERC Canada, and an National Natural Science Foundation of China grant (No. 61672336).

References


